

Scalable and formal control of reachability in qualitative networks with PINT

Loïc Paulevé

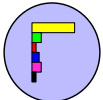
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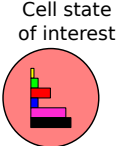
<http://loicpauleve.name>

[BC]² workshop on logical modelling of biological regulatory networks
12 September 2017

Cellular Dynamics

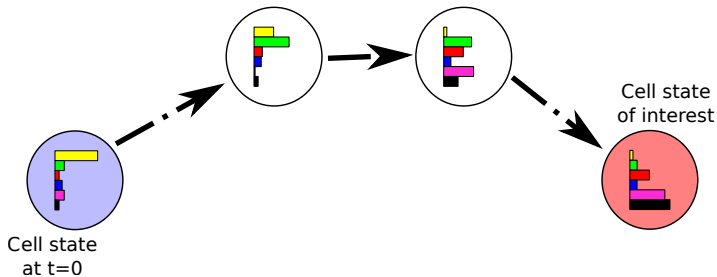


Cell state
at t=0



Initial state(s)/Goal state(s)

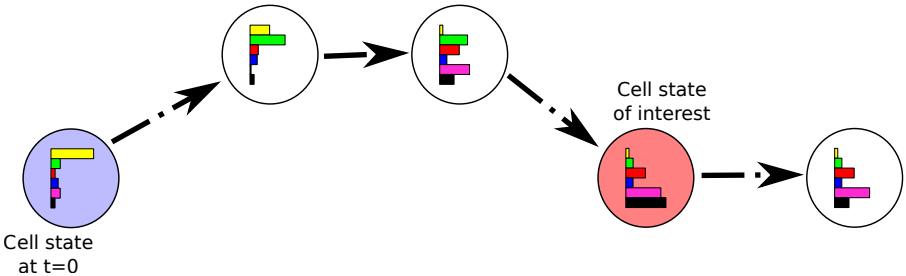
Cellular Dynamics



Initial state(s)/Goal state(s)

- Trajectory existence (reachability)

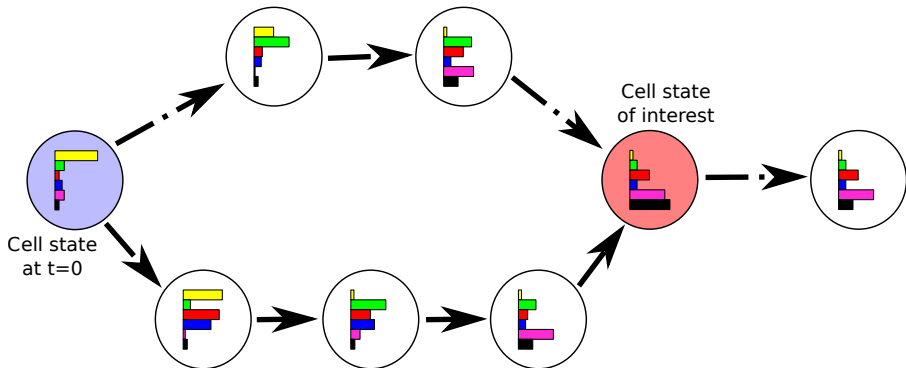
Cellular Dynamics



Initial state(s)/Goal state(s)

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Cellular Dynamics



Initial state(s)/Goal state(s)

- Trajectory existence (reachability)
- Reasoning on all trajectories: e.g., **common features**
- Control: **perturbations** to avoid/enforce goal reachability

Analysis with the software PINT

Settings

- **Qualitative models:** state of components is Boolean/with a few levels
- Consider sets of initial conditions
- **Goal states** specified by the activity of narrow number of components (**markers**)

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Contribution

- **Avoid *in silico* screening** of candidate perturbation
- Static analysis of traces: instead of computing (symbolic) state transition graph
PINT computes a **compact abstraction** of it [Paulevé et al in *Math Struct in Comp Sci* 2012]
- Results are **formal** (guaranteed) but can be incomplete due to the abstraction

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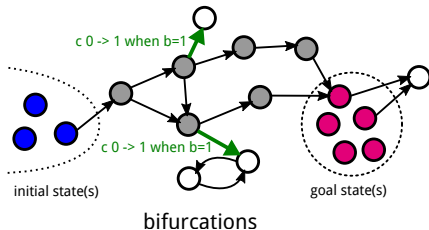
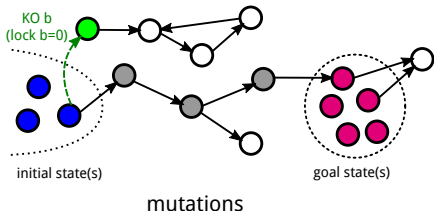
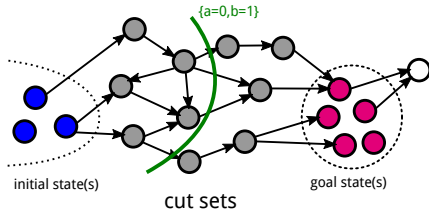
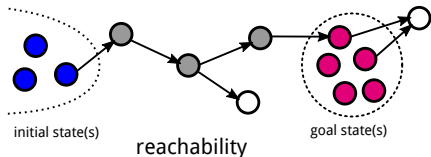
- **Avoid *in silico* screening** of candidate perturbation
- Static analysis of traces: instead of computing (symbolic) state transition graph
PINT computes a **compact abstraction** of it [Paulevé et al in Math Struct in Comp Sci 2012]
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Model input for PINT

- Main framework: **automata networks** (transition-centered specification)
- **Boolean networks**, multi-valued networks, 1-bounded Petri nets, ...
- Uses BioLQM [Naldi et al] to import **GINsim**, **SBML-Qual**, **BoolSim**, ...
+ other custom importations (BIOCHAM, SBGN-PD, ...)

Remark: the **following results do not depend on the updating schedule**
(a)synchronous)

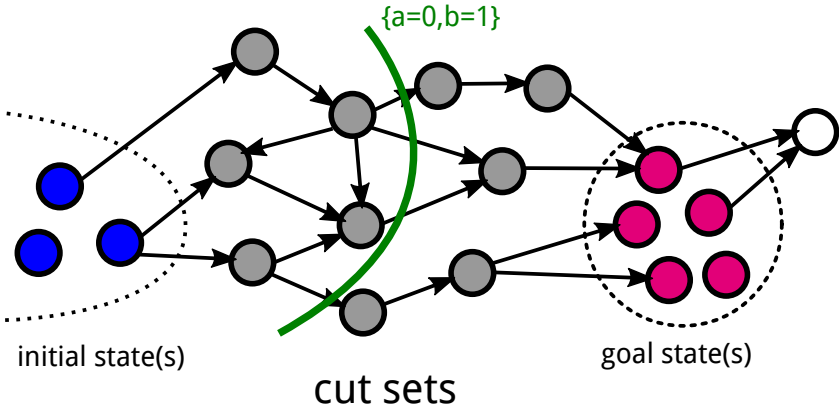
Static analysis of automata networks with Pint



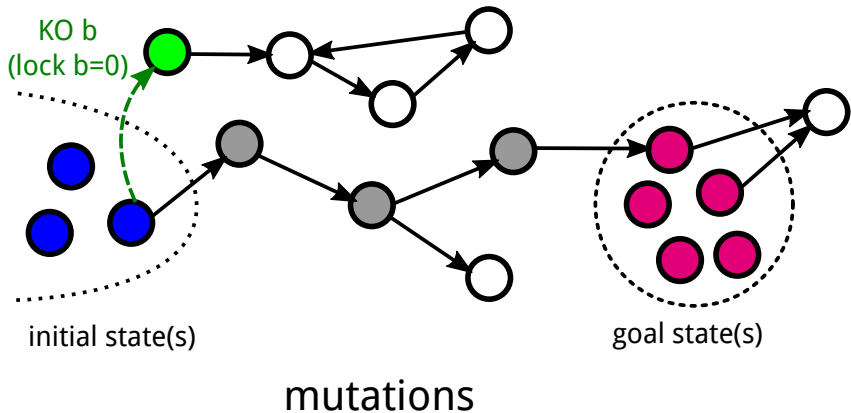
Software Pint - <http://loicpauleve.name/pint> [Paulevé at CMSB 2017]

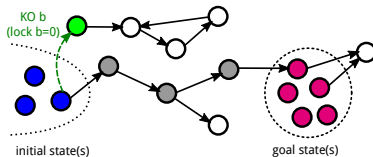
Scalability: networks with 100 - 10,000 components

Static analysis of automata networks with Pint



Static analysis of automata networks with Pint





Definition

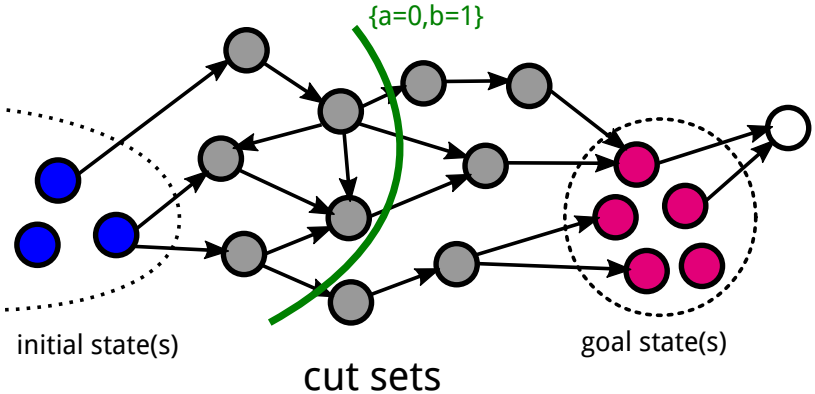
- Set of nodes with value to **lock**. E.g., $\{\text{lock}(b = 0), \text{lock}(c = 1)\}$.
- **Goal is not reachable** when applied to the initial state.

Implementation in PINT

- **Answer-Set Programming (ASP)** – similar to SAT.
- Encodes **jointly the (abstracted) dynamics and the mutation property**.
- **Solutions are derived** from the ASP logical model
 \Rightarrow **no screening**.

(PINT approximates a PSPACE-complete problem into an NP problem)

Cut sets: common features of traces to goal

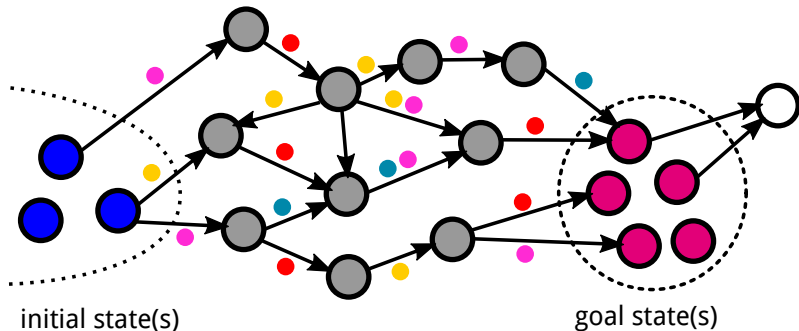


Interpretation: any trace requires at some point either $a = 0$ or $b = 1$.

Cut sets in the state transition graph

- From classical graph theory on labeled (multiple) directed graph
- Cut set = set of labels which **disconnects** initial states and goal states

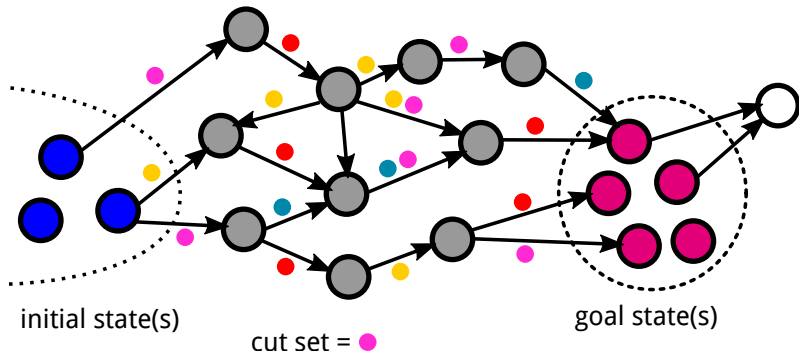
Labeled directed graph:



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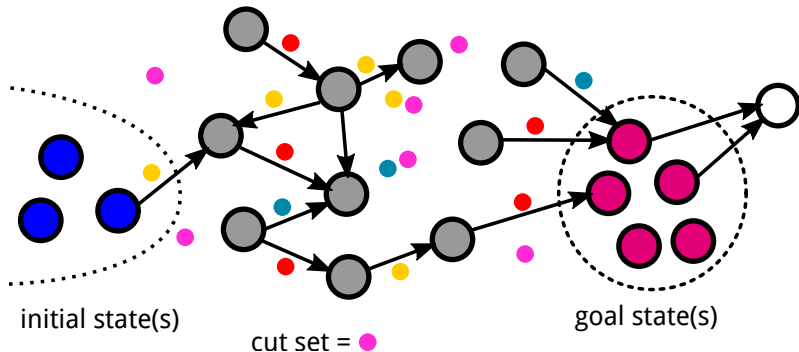
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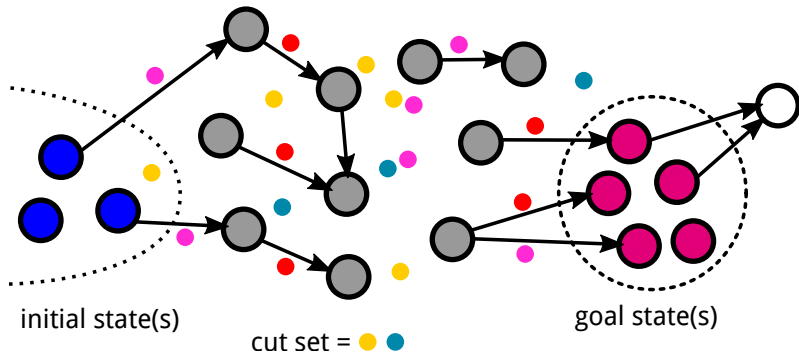
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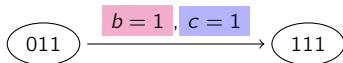


Transitions labels for Boolean networks

Labels = **minimal** cause of transitions

$$f_a(x) = x_b \text{ or } x_c$$

Labels for the transition $\langle 011 \rangle \rightarrow \langle 111 \rangle$

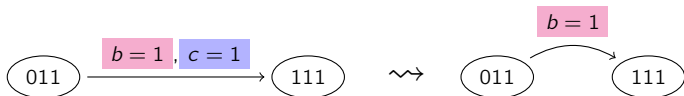


Remark: these labels come for free with automata networks/Petri nets

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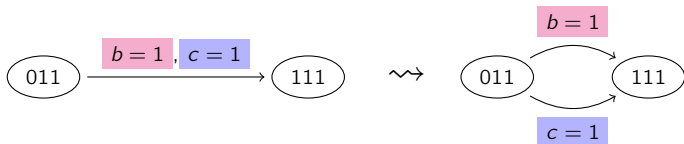
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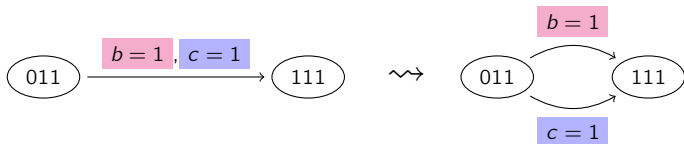
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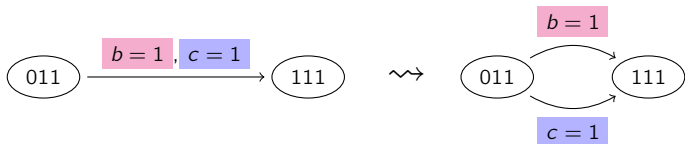
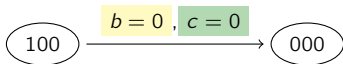
Labels for the transition $\langle 011 \rangle \rightarrow \langle 111 \rangle$ 
 \Rightarrow **1 cut set** to disconnect $\langle 011 \rangle$ and $\langle 111 \rangle$: $\{ b = 1, c = 1 \}$.

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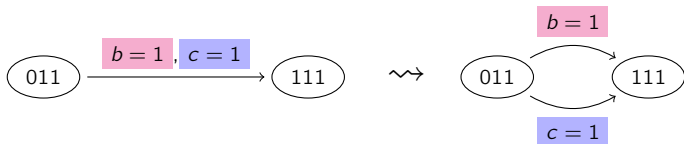
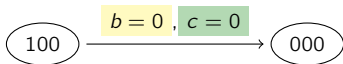
Labels for the transition $\langle 011 \rangle \rightarrow \langle 111 \rangle$ 
 \Rightarrow **1 cut set** to disconnect $\langle 011 \rangle$ and $\langle 111 \rangle$: $\{ b = 1, c = 1 \}$.
Labels for the transition $\langle 100 \rangle \rightarrow \langle 000 \rangle$ 

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Transitions labels for Boolean networks

Labels = **minimal cause of transitions**

$$f_a(x) = x_b \text{ or } x_c$$

Labels for the transition $\langle 011 \rangle \rightarrow \langle 111 \rangle$ 
 \Rightarrow **1 cut set** to disconnect $\langle 011 \rangle$ and $\langle 111 \rangle$: $\{ b = 1, c = 1 \}$.
Labels for the transition $\langle 100 \rangle \rightarrow \langle 000 \rangle$ 
 \Rightarrow **2 cut sets** to disconnect $\langle 100 \rangle$ and $\langle 000 \rangle$: $\{ b = 0 \}$, $\{ c = 0 \}$.

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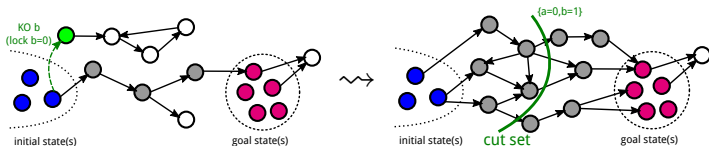
Cut sets in PINT

Implementation

- Does not build the state transition graph.
- **Dedicated algorithm** on its abstraction (3-partite graph) [Paulevé et al at CAV 2013].
- **Solutions are derived**, no candidate enumeration (**no screening**).

An alternative implementation with ASP could be considered as well.

Mutations vs Cut sets



From mutations to cut sets

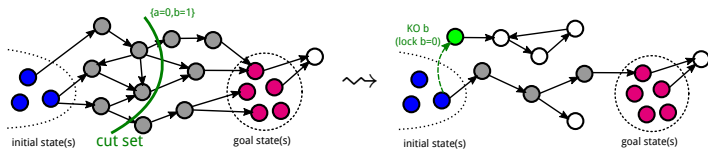
- $\text{lock}(a = i)$ cuts transitions using $a = j, j \neq i$
- To any mutation set corresponds a cut set
- ... but for a potentially different initial state

E.g., consider the mutation set

$$\{\text{lock}(b = 0), \text{lock}(c = 1)\} \\ \Rightarrow \{b = 1, c = 0\}$$

is a cut set for the goal from the initial state with $b = 0$ and $c = 1$.

Mutations vs Cut sets



From cut sets to mutations

- Idea: if every trace to goal uses either $a = 1$ or $c = 1$, KO of a and b prevents goal reachability
- ... *but* a cut set can include both active and inactive state of a same node
- ... the mutation should not change the initial state.

⇒ a cut set does not always gives a mutation

E.g., considering the initial state $\langle a = 0, b = 1, c = 0 \rangle$,

- $\{a = 1, c = 1\}$ gives guaranteed mutation $\{\text{lock}(a = 0), \text{lock}(c = 0)\}$;
- $\{a = 1, a = 0, b = 0\}$ gives no mutation;
- $\{a = 1, b = 1\}$ gives non-proven mutation $\{\text{lock}(a = 0), \text{lock}(b = 0)\}$.

Scalability of implementations

Computations with PINT:

- k -cut sets: OCaml implementation (algorithm on abstract structure)
- k -mutations: Answer-Set Programming (ASP) with clingo

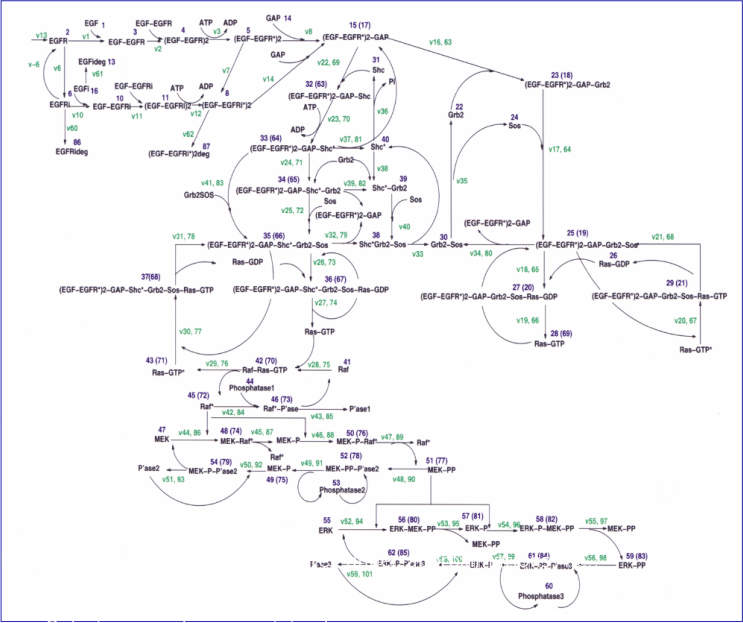
k : limit results to sets with at most k elements.

Goal	TCell-d (101) FOXP3=1		MAPK (309) ERK-PP=1		PID (10,229) SNAIL=1	
3-cut sets	0.06s	35	0.06s	24	1.2s	7
4-cut sets	0.10s	101	0.1s	48	5s	37
6-cut sets	0.60s	495	1s	60	10m	907
3-mutations	0.30s	15	5s	222	50m	7
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6-mutations	0.30s	15	Too many		50m	367

TCell-d: Abou-Jaoudé et al. in *Frontiers in Bioengin. and Biotech*, 2015

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Important remark: PINT computes **under-approximations**, i.e.,

- Solutions can be missed
- Solutions can be non-minimal

There is a [public instance of Jupyter/pint](http://tmpnb.loicpauleve.name) at
`http://tmpnb.loicpauleve.name`

Be aware that

- For short tests only (limited session durations)
- It runs in a virtual machine with limited resources on a personal server

You can install Pint locally either with binary packages or using docker
`http://loicpauleve.name/pint/doc/`

Mutations vs Cut sets from initial states to goal states

- Mutations: block reachability of the goal
- Cut sets: common features of all the trajectories to the goal
- Mutations give cut sets, but (some are) for different initial states
- Some cut sets cannot be transformed into mutations
(if they change the initial state; if they use both the active and inactive form of a node)

PINT implementation

- No screening of candidates, solutions are deduced by static analysis
- Scalable to networks $>1,000$ components
- Under-approximation (no magic)

On-going and future work

- Compute temporal mutations
- Static quantification of the effect of a partial mutation/cut sets

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LS2N, Nantes MeForBio

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